

Phoenics: A Bayesian optimizer for Chemistry

Authors: Florian Häse, Loïc M. Roch, Christoph Kreisbeck, Alán Aspuru-Guzik

Presenter: Florian Häse

Facilitators: Elham Dolatabadi, Rouzbeh Afrasiabi

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HARVARD
UNIVERSITY

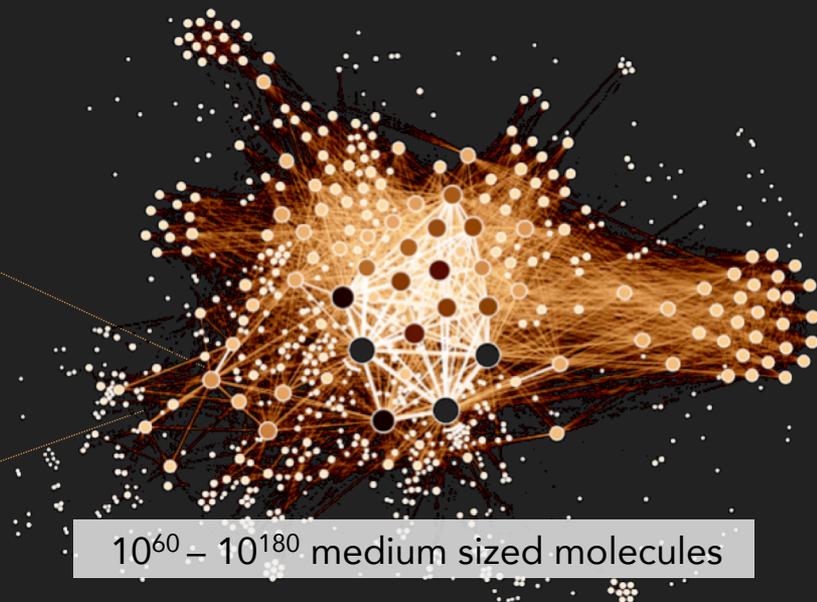
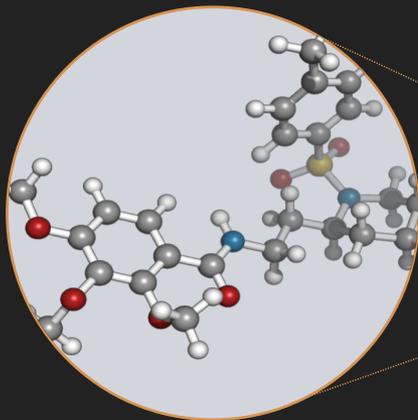


Materials challenges of the 21st century

Chemistry is the study of matter and the changes it undergoes

Functional molecules / materials promise solutions to key global challenges:

- **Clean energy**
(e.g. solar cells, flow batteries)
- **Global health**
(e.g. drugs, water purifier)
- **Sustainability**
(e.g. biodegradable plastics)
- **and many more**



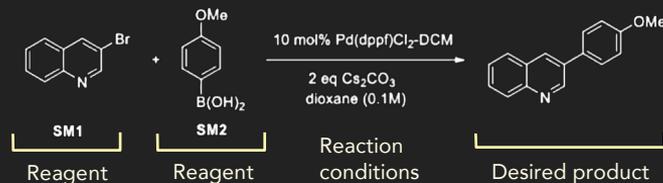
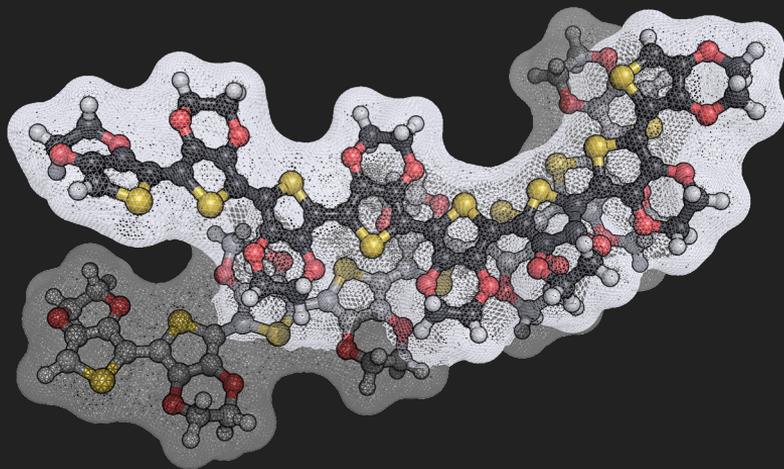
How do we find these materials?

Illustration of the molecular space

Materials challenges of the 21st century

How do we make these materials?

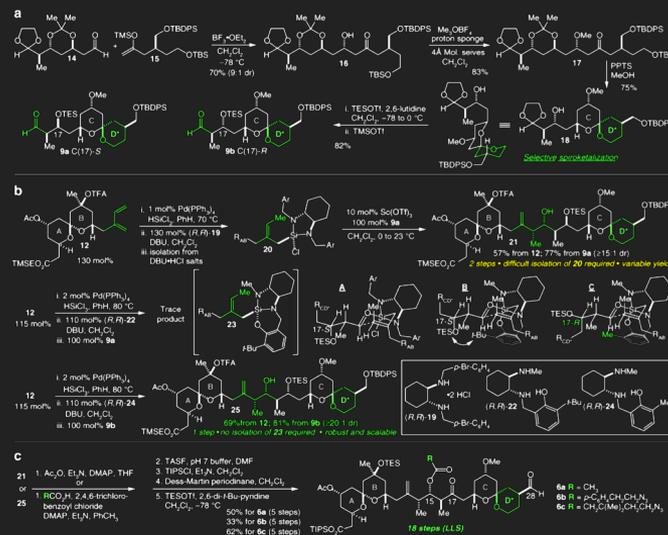
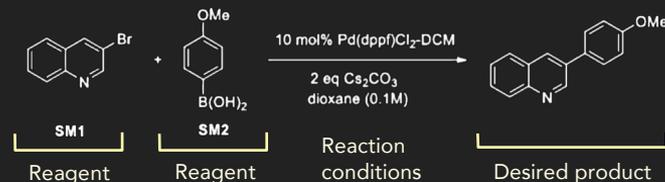
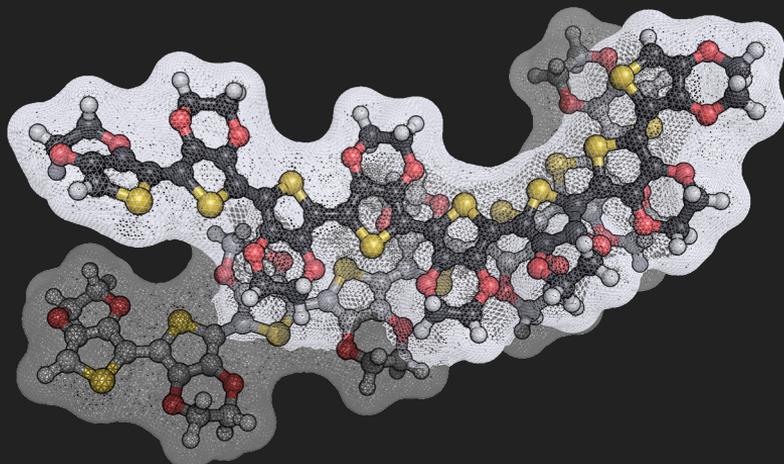
- (i). Find a synthesis route
- (ii). Find suitable reaction conditions,
(i.e. *make the reaction work*)



Materials challenges of the 21st century

How do we make these materials?

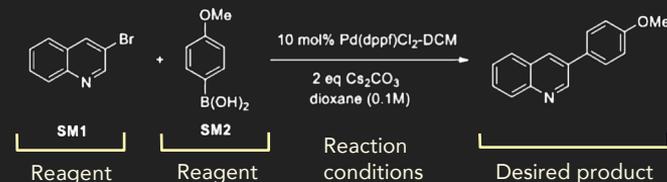
- Find a synthesis route
- Find suitable reaction conditions, (i.e. make the reaction work)



Materials challenges of the 21st century

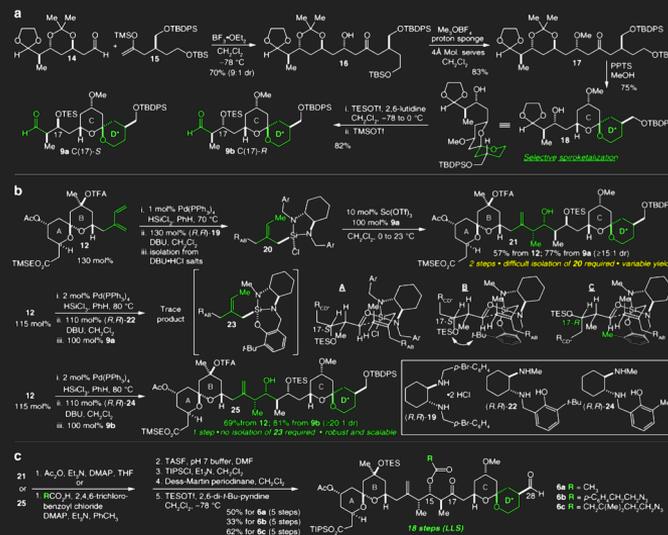
How do we make these materials?

- (i). Find a synthesis route
- (ii). Find suitable reaction conditions, (i.e. make the reaction work)



Challenges

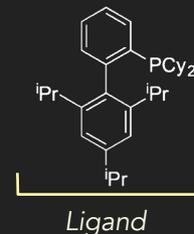
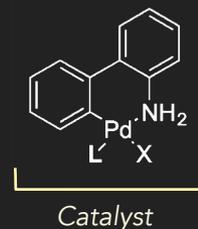
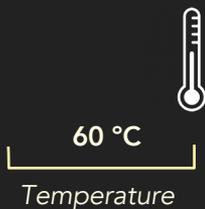
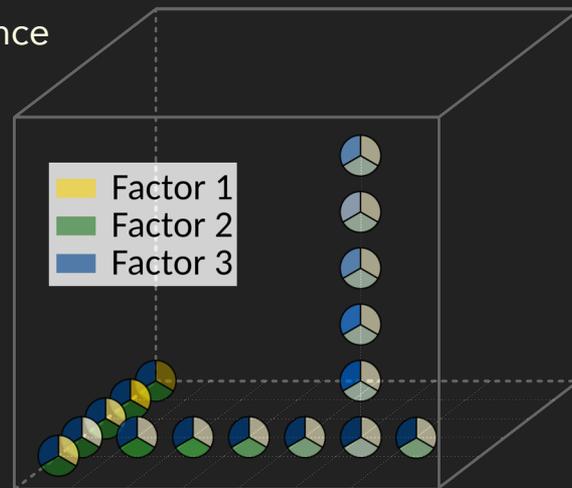
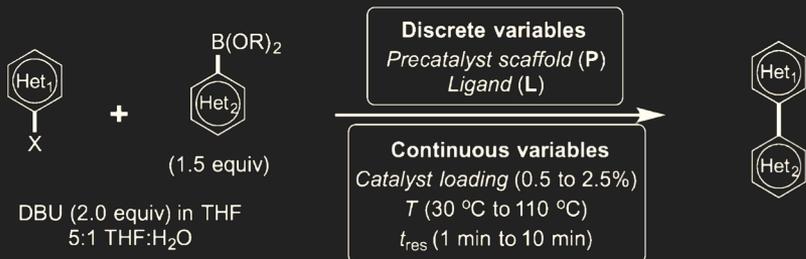
- Many parameters to tune
- Time constraints delay feedback
- Resource constraints often prevent exhaustive screening
- Large, well curated databases do not exist



Traditional routes to designing experiments

- Intuition of researchers based on prior knowledge and experience
- Systematic approaches:

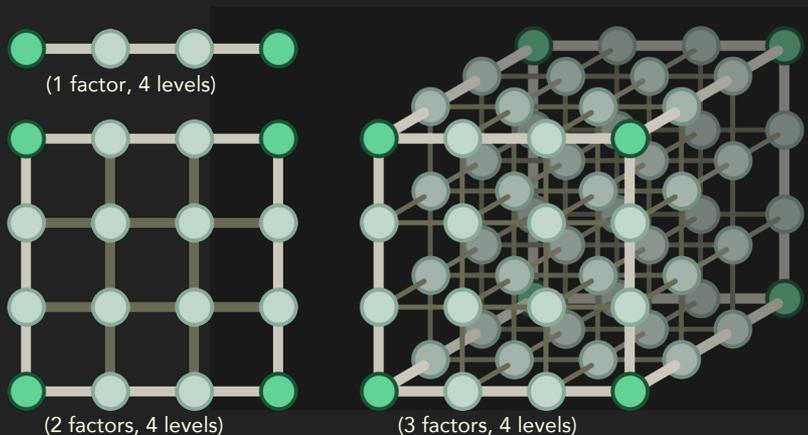
one-factor-at-a-time (OFAT)



Traditional routes to designing experiments

Design of experiments (DoE)

- Similar to grid searches
- Probes hypothesized relations between parameters (factors) and measurements



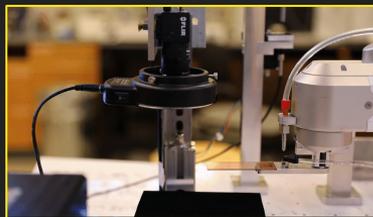
- Subsequent campaigns might be executed with finer grids

Advantage:

experiments are massively parallelizable (resource permitting)

Drawback:

design choices cannot be refined *on-the-fly*



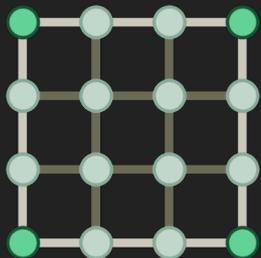
Traditional routes to designing experiments

Design of experiments (DoE)

- implicitly constructs Taylor expansion to the experimental response surface

$$f(x) = \sum_{|\alpha| < k} \frac{1}{\alpha!} \frac{\partial^{|\alpha|} f(x)}{\partial x_1^{\alpha_1} \dots \partial x_n^{\alpha_n}} \bigg|_{x=\alpha} (x - \alpha)^\alpha$$

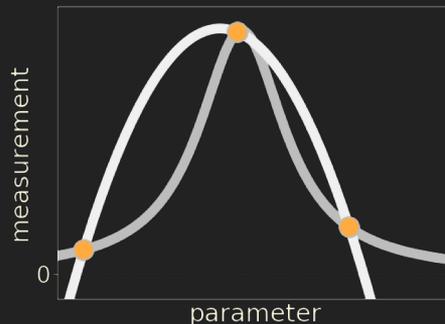
- shows adverse exponential scaling with the number of parameters



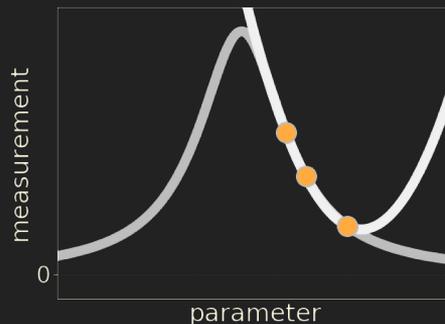
(2 factors, 4 levels)

$$\# \text{ exp} = (\# \text{ levels})^{\# \text{ parameters}}$$

Only applicable to small spaces



— True response ● Measurement
— Interpretation



Physical constraints can be violated

Misleading trends might be detected

Experimental campaign is executed without constant refinement

Rethinking the experimentation process

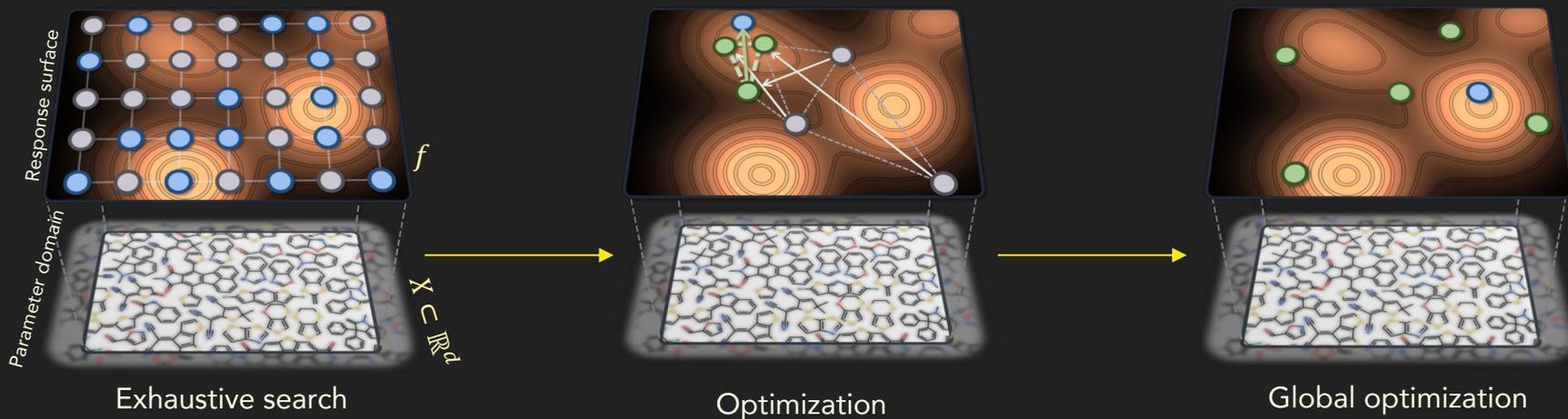
Alternative approaches

- formulate experiment planning as an optimization problem

$$\mathbf{x}^* = \operatorname{argmin}_{\mathbf{x} \in X \subset \mathbb{R}^d} f(\mathbf{x})$$

Assumptions about f :

- evaluations expensive (take minutes, hours, days)
- evaluations are noisy
- f is mostly well-behaved
- f is defined on a moderately large space ($d \leq 20$)

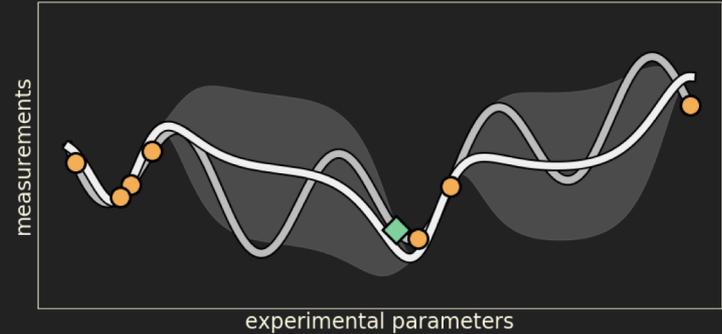


Bayesian optimization

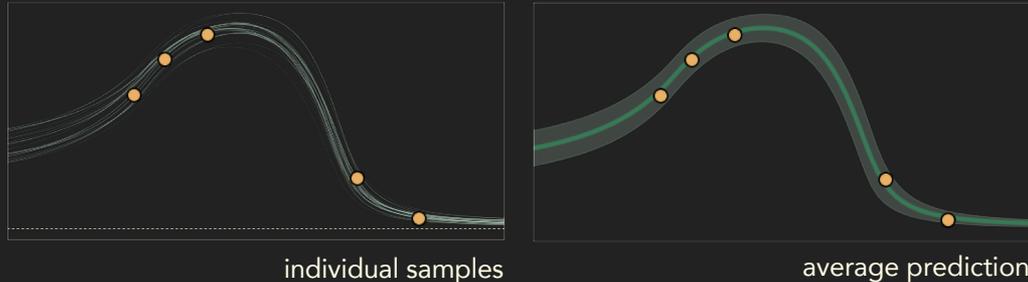
Bayesian optimization relies on *probabilistic universal function approximators*.

The *true response surface* is modelled as the *maximum likelihood estimate* of the *distribution of functions*.

Bayesian optimization with Gaussian processes



Regression with a Bayesian neural network



Assumptions about f :

- evaluations expensive (minutes, hours, days)
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Bayesian optimization

- (i). Construct a surrogate using a model which provides uncertainty information

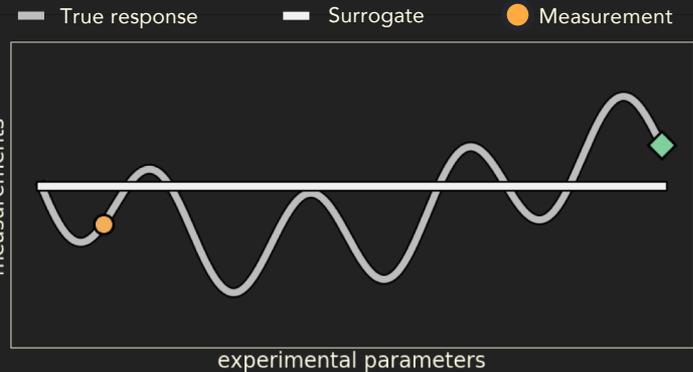
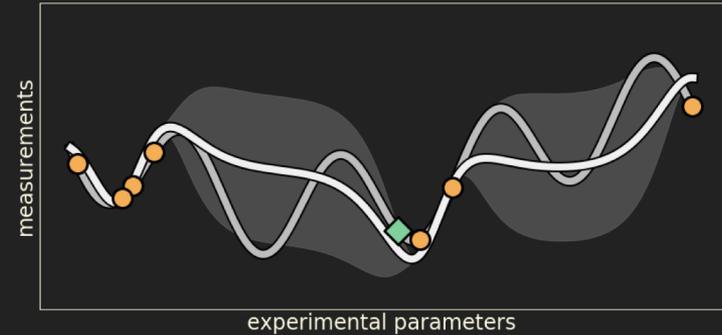
Gaussian processes, random forests, Bayesian neural networks, etc.

- (ii). Formulate an acquisition function which balances space exploration and knowledge exploitation

expected improvement, upper confidence bound, entropy search

- (iii). Speculate about the information gain when evaluating parameters and suggest the most promising

Bayesian optimization with Gaussian processes



[1] Snoek, J., Larochelle, H., & Adams, R. P. (2012). Practical bayesian optimization of machine learning algorithms.

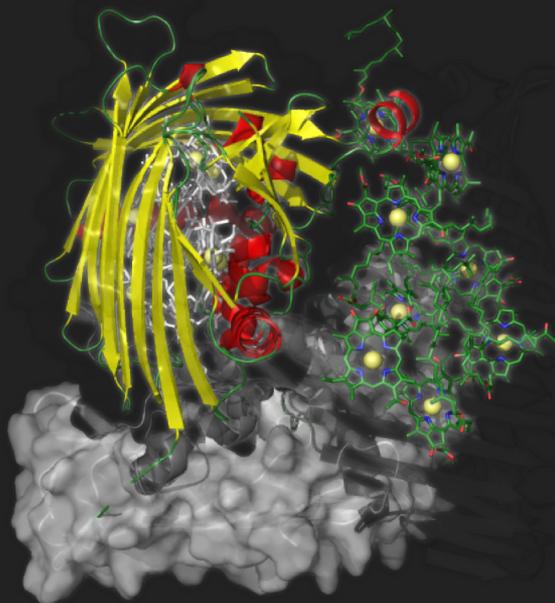
In *Advances in neural information processing systems* (pp. 2951-2959).

[2] Frazier, Peter I. "A tutorial on Bayesian optimization." *arXiv preprint arXiv:1807.02811* (2018).

[3] Hutter, Frank, Holger H. Hoos, and Kevin Leyton-Brown. "Sequential model-based optimization for general algorithm configuration." *International Conference on Learning and Intelligent Optimization*. Springer, Berlin, Heidelberg, 2011.

A brief introduction to metadynamics

Molecular dynamics is a computational approach to simulate the dynamics of *many-particle systems*, e.g. biologically relevant protein complexes at atomic resolution.

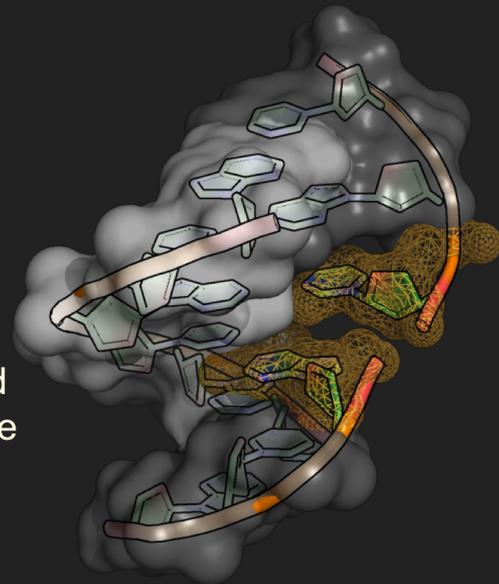


Typically 100,000s atoms and more than 10^9 integration steps

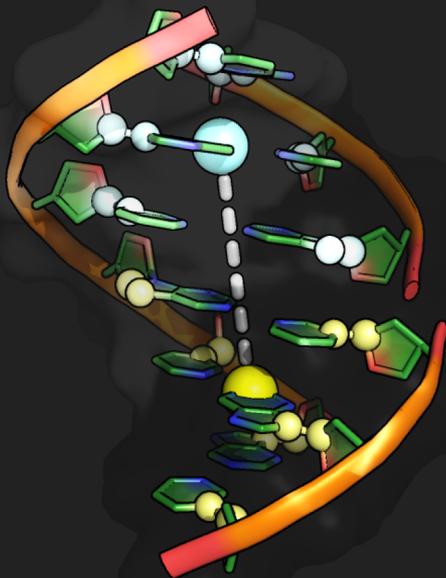
$$\mathbf{F}(\mathbf{r}) = -\nabla U(\mathbf{r}) = m\dot{\mathbf{v}}(t)$$

$$\mathbf{v}(t) = \dot{\mathbf{r}}(t)$$

Metadynamics describes an enhanced sampling method to reduce the runtime of molecular dynamics simulations.

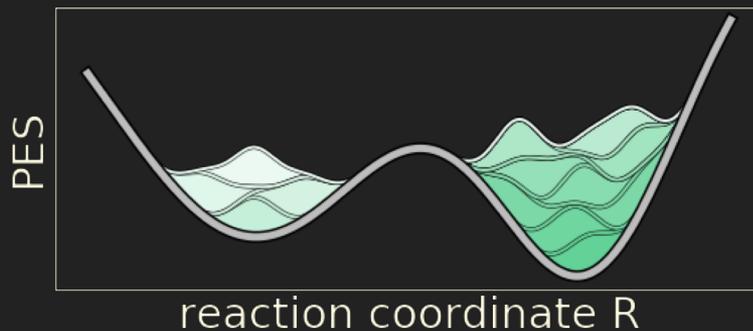


A brief introduction to metadynamics

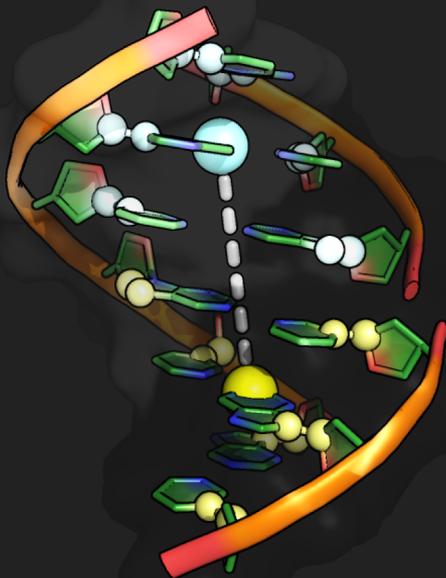


Exploration of the potential energy surface (PES) is encouraged by adding penalty terms to previously visited regions.

$$\text{PES}_{\text{eff}}(\mathbf{r}, t) = \text{PES}(\mathbf{r}) + \int_0^t dt' \omega \exp\left(-\frac{\mathbf{R}(\mathbf{r}) - \mathbf{R}(\mathbf{r}(t')))^2}{2\sigma^2}\right)$$

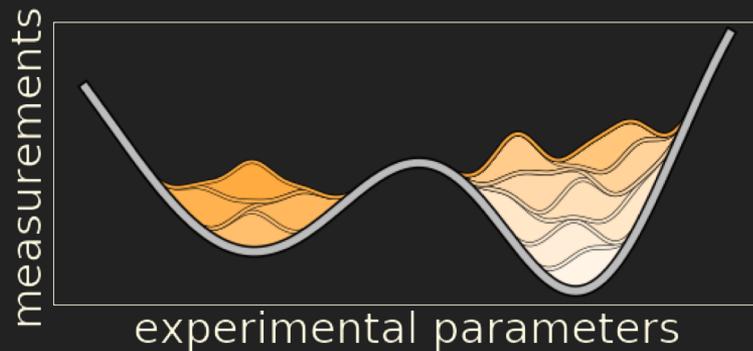


A brief introduction to metadynamics



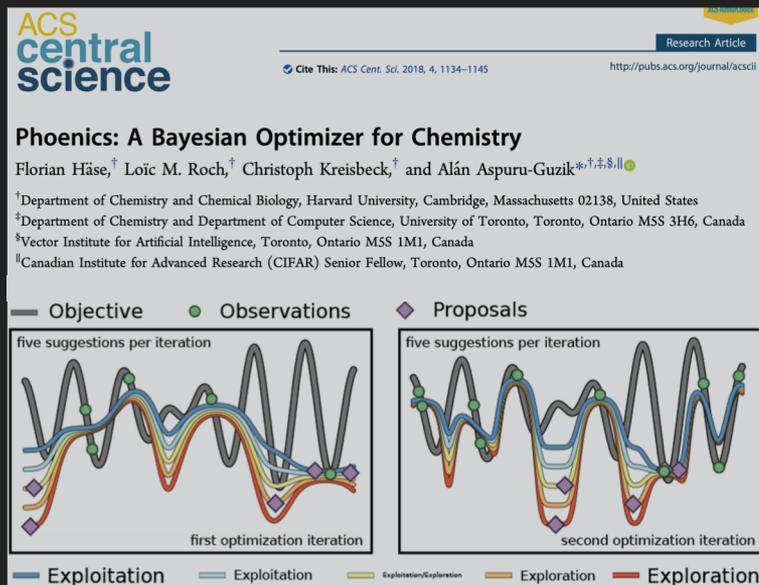
Can we use similar ideas to determine the optimal parameters for an experiment?

$$\text{PES}_{\text{eff}}(\mathbf{r}, t) = \text{PES}(\mathbf{r}) + \int_0^t dt' \omega \exp\left(-\frac{\mathbf{R}(\mathbf{r}) - \mathbf{R}(\mathbf{r}(t')))^2}{2 \sigma^2}\right)$$

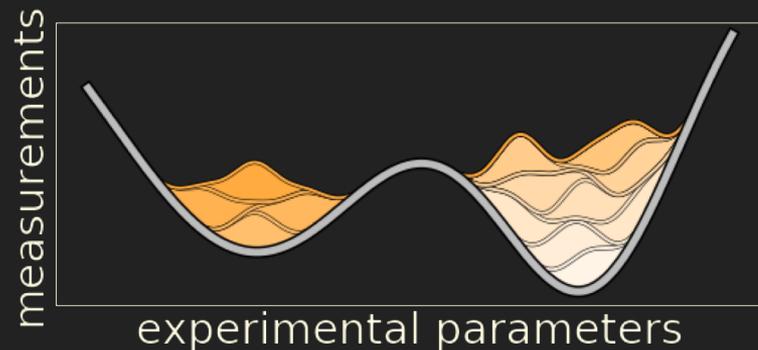


Phoenics: A Bayesian optimizer for chemistry

Phoenics implements global optimization by combining ideas from Bayesian optimization with concepts from Bayesian kernel density estimation.



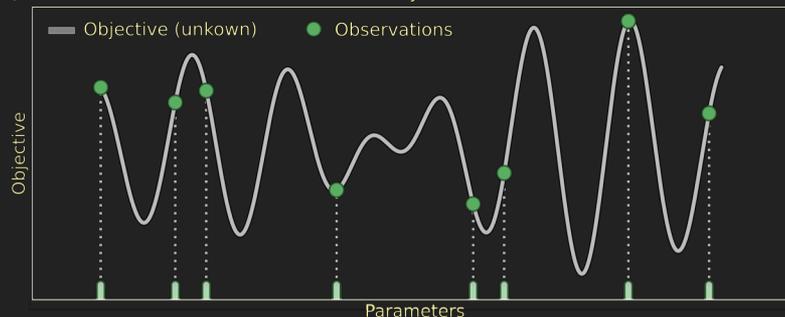
- natively supports batch optimization
- favorable linear scaling with the number of measurements



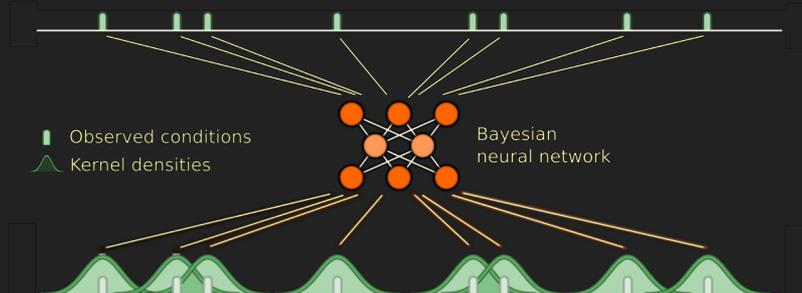
Phoenics: A Bayesian optimizer for chemistry

Phoenics implements a four-step process to propose experimental parameters for future evaluation.

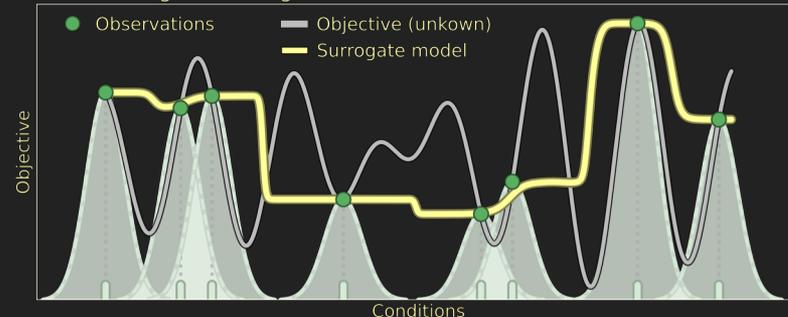
A) Available observations and unknown objective



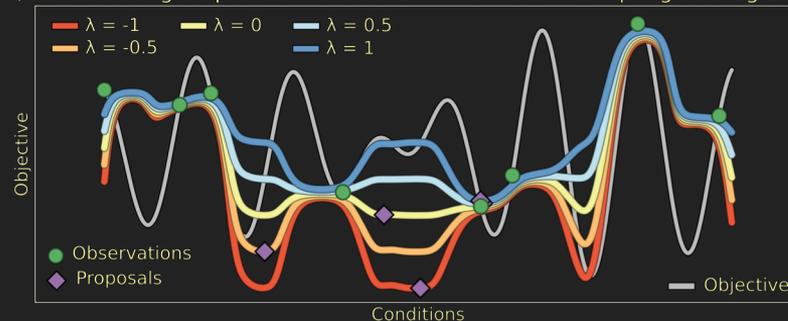
B) Estimation of kernel densities



C) Constructing the surrogate from the kernel densities



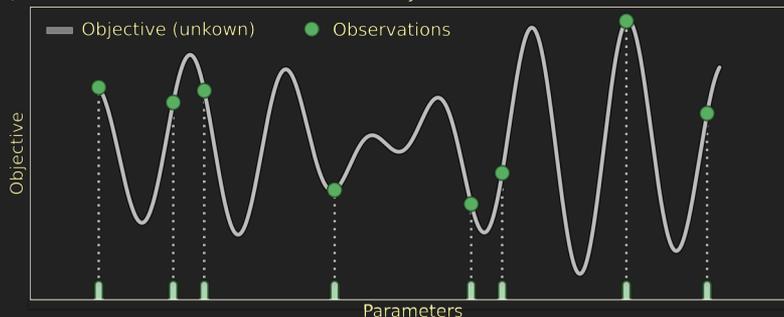
D) Constructing acquisition functions with different sampling strategies



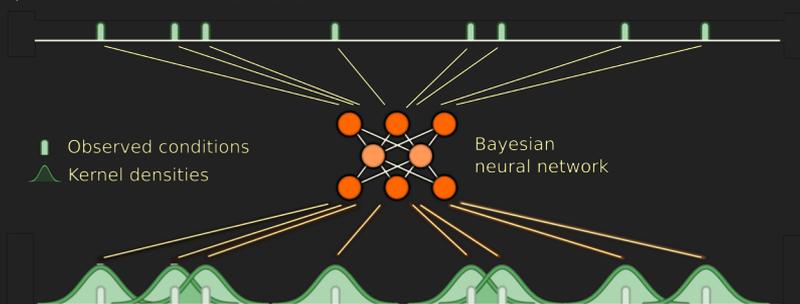
Phoenics: A Bayesian optimizer for chemistry

Phoenics estimates parameter kernel densities using a Bayesian neural network:

A) Available observations and unknown objective



B) Estimation of kernel densities



Posterior kernel densities are modeled with variational probability distributions, where

$$p(\mathbf{x}_i | \theta, \{\mathbf{x}_0, \dots, \mathbf{x}_n\}) = \text{Normal}(\mathbf{x}_i | \text{BNN}(\mathbf{x}_i; \theta), \sigma^2)$$

with

$$\phi_1(\mathbf{x}_i) = \tanh(\mathbf{x}_i \cdot \mathbf{w}_0 + \mathbf{b}_0)$$

$$\phi_2(\phi_1) = \tanh(\phi_1 \cdot \mathbf{w}_1 + \mathbf{b}_1)$$

$$\text{BNN}(\phi_2) = \text{sigmoid}(\phi_2 \cdot \mathbf{w}_2 + \mathbf{b}_2)$$

and priors are chosen as

$$\mathbf{w}_k \sim \text{Normal}(0, \mathbf{I})$$

$$\mathbf{b}_k \sim \text{Normal}(0, \mathbf{I})$$

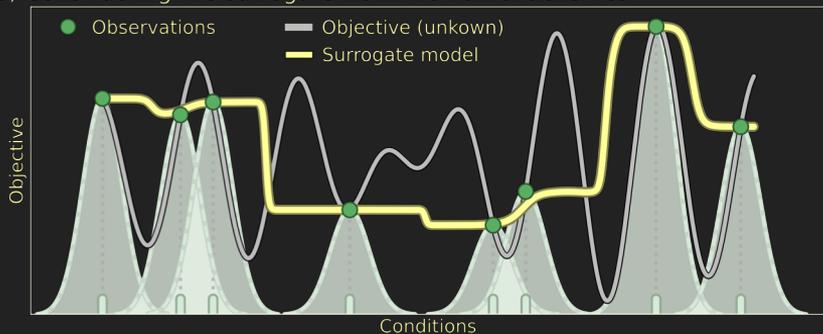
Phoenics: A Bayesian optimizer for chemistry

The kernel densities provide the basis for the surrogate.

Given a set of n observations

$$D_n = \{(\mathbf{x}_k, f_k)\}_{k=1}^n$$

C) Constructing the surrogate from the kernel densities



Note, that

$$\sigma^2 = 1/\tau, \quad \tau \sim \text{Gamma}(n^2, 1)$$

the surrogate is constructed similar to a *partition function*

$$\alpha(\mathbf{x}) = \frac{\sum_{k=1}^n f_k p_k(\mathbf{x})}{\sum_{k=1}^n p_k(\mathbf{x})}$$

where

$$\begin{aligned} p_k(\mathbf{x}) &= p_k(\mathbf{x}|\theta, \{\mathbf{x}_0, \dots, \mathbf{x}_n\}) \\ &= \text{Normal}(\mathbf{x}_i | \text{BNN}(\mathbf{x}_i; \theta), \sigma^2) \end{aligned}$$

and

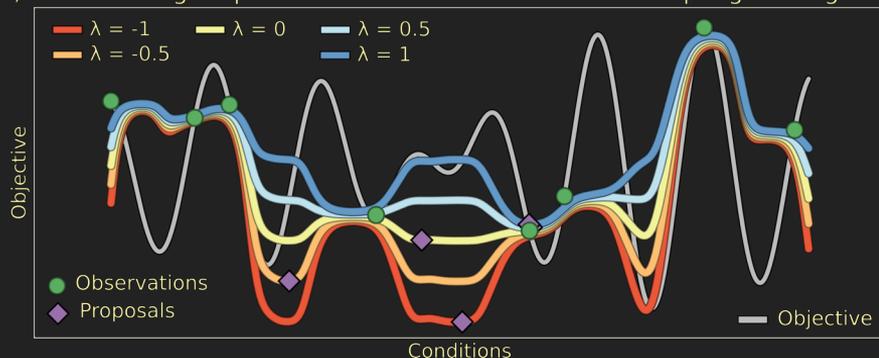
$$\alpha(\mathbf{x}) \cong p_k(\mathbf{x}) \quad \text{for} \quad \mathbf{x} \cong \mathbf{x}_k$$

where the approximation becomes exact in the limit of infinitely many distinct observations.

Phoenics: A Bayesian optimizer for chemistry

The kernel densities provide the basis for the surrogate.

D) Constructing acquisition functions with different sampling strategies



Without any prior knowledge, the **optimum** \mathbf{x}^* could be located **anywhere** in the domain $\mathbf{X} \subset \mathbb{R}^d$ with **equal probability**.

$$p_{\text{prior}}(\mathbf{x} = \mathbf{x}^*) = 1/\text{Volume}(\mathbf{X}) = p_{\text{uniform}}(\mathbf{x})$$

The surrogate is inaccurate in low-density regions

$$\alpha(\mathbf{x}) = \frac{\sum_{k=1}^n f_k p_k(\mathbf{x})}{\sum_{k=1}^n p_k(\mathbf{x})}$$

Confidence can be built into the surrogate by adding $p_{\text{uniform}}(\mathbf{x})$ to indicate this lack of information

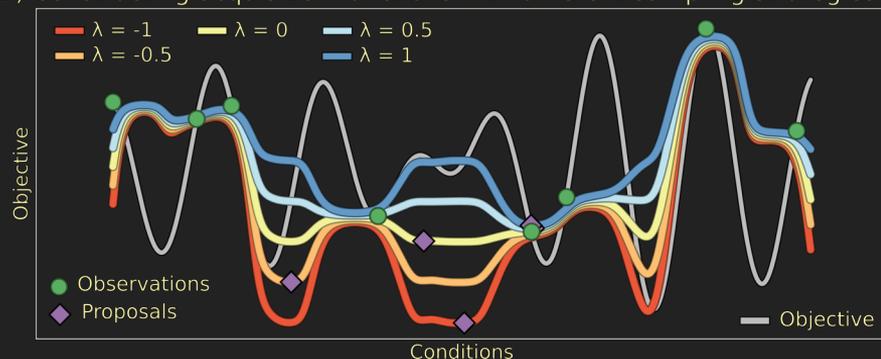
$$\alpha(\mathbf{x}) = \frac{\sum_{k=1}^n f_k p_k(\mathbf{x}) + \lambda p_{\text{uniform}}(\mathbf{x})}{\sum_{k=1}^n p_k(\mathbf{x}) + p_{\text{uniform}}(\mathbf{x})}$$

The number of evaluations of the Bayesian network is independent of the number of evaluations of this acquisition function.

Phoenics: A Bayesian optimizer for chemistry

The kernel densities provide the basis for the surrogate.

D) Constructing acquisition functions with different sampling strategies



Suggesting parameters with different sampling strategies, e.g. $\lambda \in \{-1, 0, 1\}$, only requires one kernel density estimation.

The surrogate now contains a sampling parameter $\lambda \in \mathbb{R}$ indicating the trust we put in the prior

$$\alpha(\mathbf{x}) = \frac{\sum_{k=1}^n f_k p_k(\mathbf{x}) + \lambda p_{\text{uniform}}(\mathbf{x})}{\sum_{k=1}^n p_k(\mathbf{x}) + p_{\text{uniform}}(\mathbf{x})}$$

When suggesting parameters based on the global optimum of the surrogate $\alpha(\mathbf{x})$:

- $\lambda < 0$ biases towards explorative behavior
- $\lambda > 0$ biases towards exploitative behavior

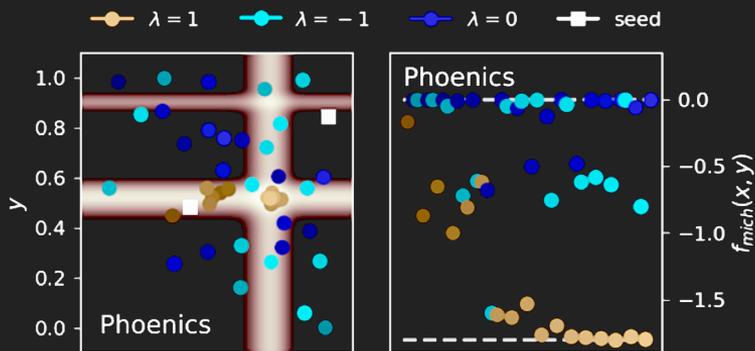
Break



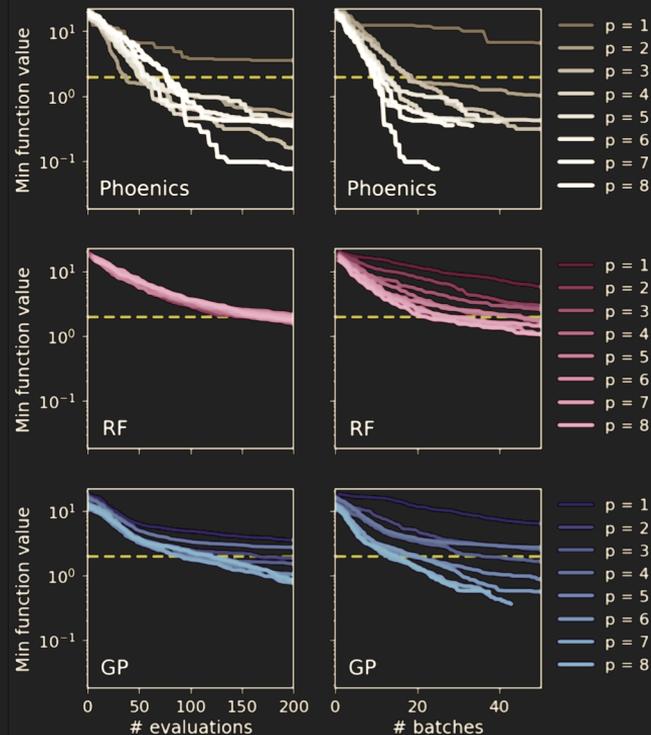
Performance on analytic benchmarks

Benchmarks on 15 different analytic functions in two and higher dimensions

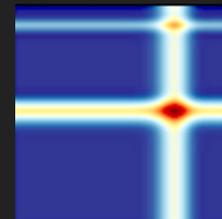
- Compared to *spearmint* (GP), *SMAC* (RF), *particle swarm search* and *CMA-ES* (not shown)
- only slightly outperformed by *spearmint* on purely convex functions



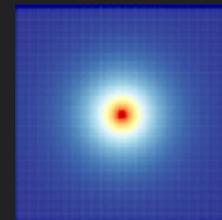
Optimization on the two-dimensional *Michalewicz* function



Optimization on the two-dimensional *Ackley path* function



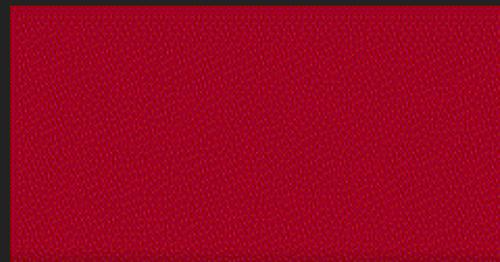
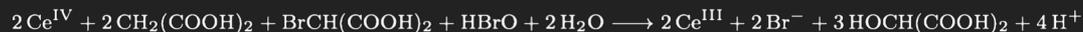
Michalewicz function



Ackley path function

(i) Chemical oscillators

Scheme 1. Subreactions of the Belousov–Zhabotinsky Reaction⁷⁸



Goal: finding parameters which yield a desired dynamic behavior

The reaction dynamics can be described with a set of coupled non-linear differential equations (*Oregonator*)* with 11 parameters

$$\frac{dX}{dt} = k_1AY - k_2XY + k_3BX - 2k_4X^2$$

$$\frac{dY}{dt} = -k_1AY - k_2XY + fk_5Z$$

$$\frac{dZ}{dt} = k_3BX - k_5Z$$

Non-dimensionalizing these equations yields three effective concentrations (α, η, ρ) and 4 independent effective reaction rates (s, q, w, f)

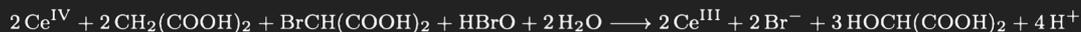
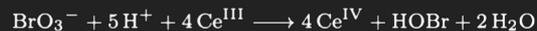
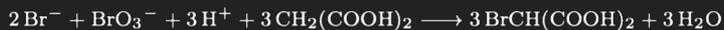
$$\frac{d\alpha}{d\tau} = s(\eta - \eta\alpha + \alpha - q\alpha^2)$$

$$\frac{d\eta}{d\tau} = s^{-1}(-\eta - \eta\alpha + f\rho)$$

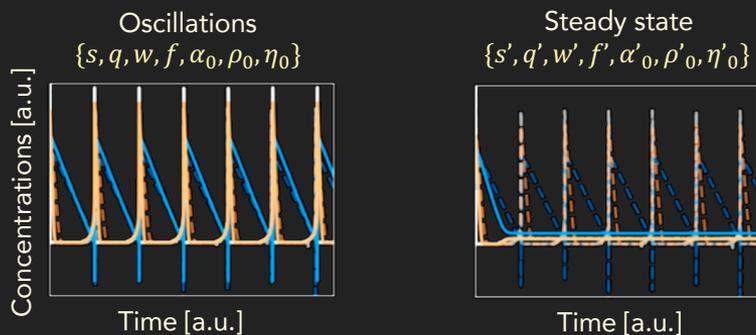
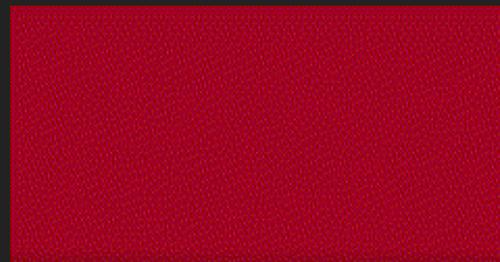
$$\frac{d\rho}{d\tau} = w(\alpha - \rho)$$

(i) Chemical oscillators

Scheme 1. Subreactions of the Belousov–Zhabotinsky Reaction⁷⁸



Goal: finding parameters which yield a desired dynamic behavior



- - α (target) - - - η (target) - - - ρ (target)
 — α (sampled) — η (sampled) — ρ (sampled)

Non-dimensionalizing these equations yields three effective concentrations (α, η, ρ) and 4 independent effective reaction rates (s, q, w, f)

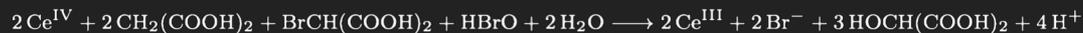
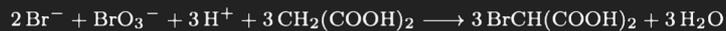
$$\frac{d\alpha}{d\tau} = s (\eta - \eta\alpha + \alpha - q\alpha^2)$$

$$\frac{d\eta}{d\tau} = s^{-1} (-\eta - \eta\alpha + f\rho)$$

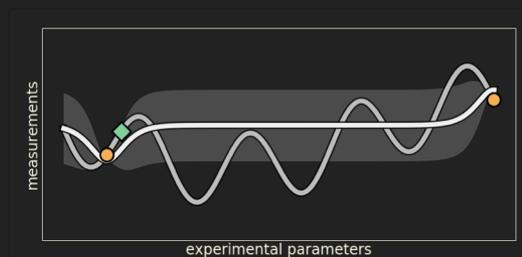
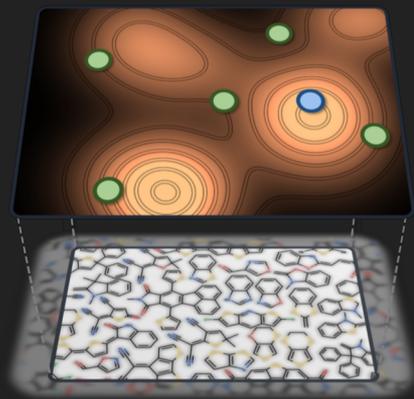
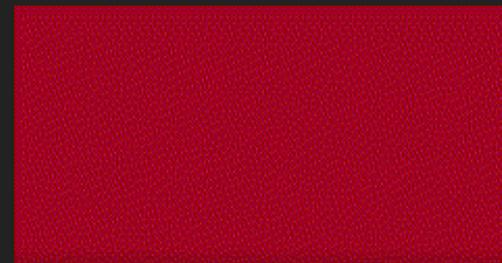
$$\frac{d\rho}{d\tau} = w (\alpha - \rho)$$

(i) Chemical oscillators

Scheme 1. Subreactions of the Belousov–Zhabotinsky Reaction⁷⁸

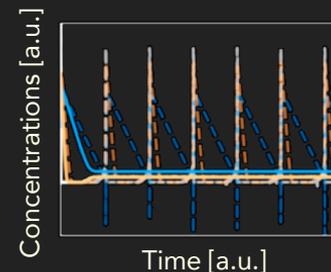


Goal: finding parameters which yield a desired dynamic behavior



run experiment

$\{s, q, w, f, \alpha_0, \rho_0, \eta_0\}$

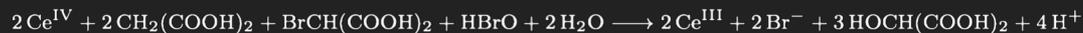
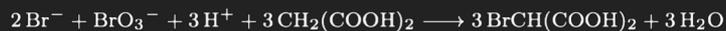


determine merit of suggested parameters

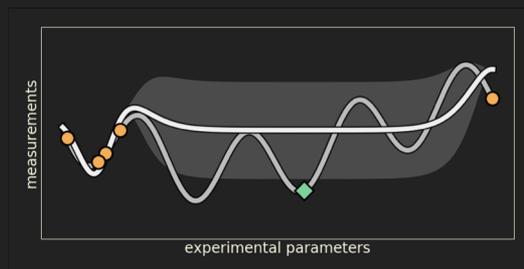
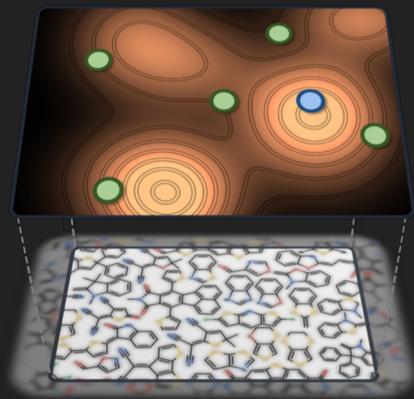
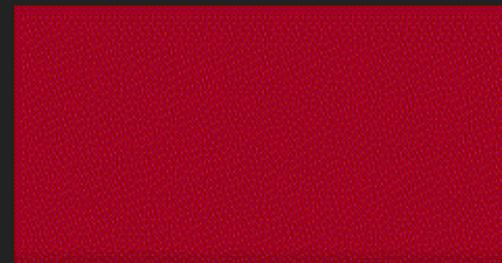
-- α (target) - - - η (target) - - - ρ (target)
 — α (sampled) — η (sampled) — ρ (sampled)

(i) Chemical oscillators

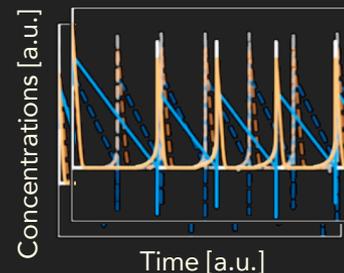
Scheme 1. Subreactions of the Belousov–Zhabotinsky Reaction⁷⁸



Goal: finding parameters which yield a desired dynamic behavior



$\{s, q, w, f, \alpha_0, \rho_0, \eta_0\}$

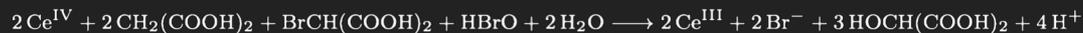
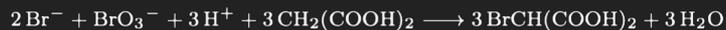


determine merit of suggested parameters

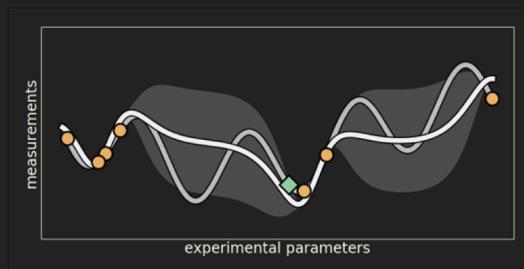
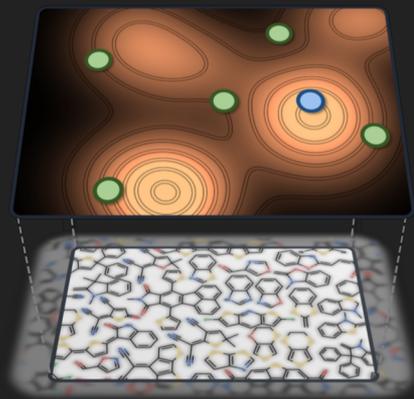
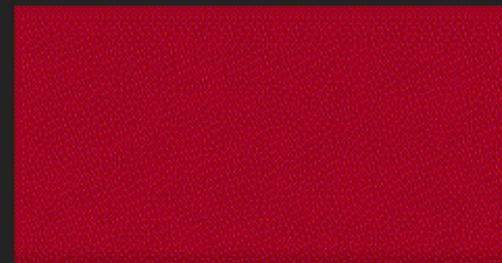
-- α (target) - - - η (target) - - - ρ (target)
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(i) Chemical oscillators

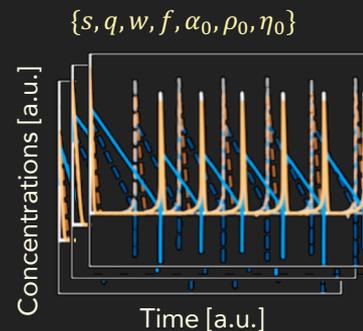
Scheme 1. Subreactions of the Belousov–Zhabotinsky Reaction⁷⁸



Goal: finding parameters which yield a desired dynamic behavior



run experiment →

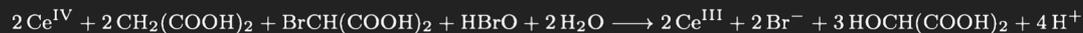
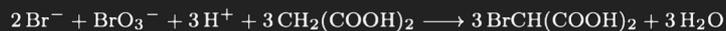


↑ determine merit of suggested parameters

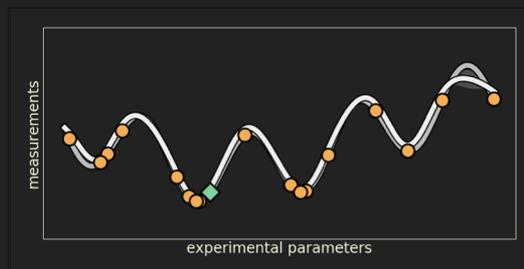
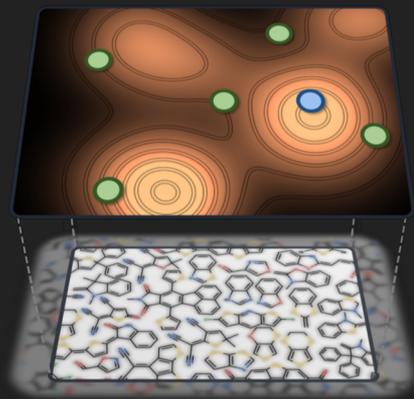
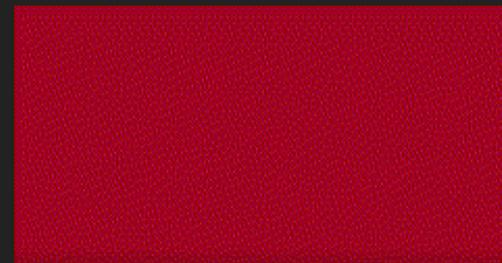
--	α (target)	- - -	η (target)	- - -	ρ (target)
—	α (sampled)	—	η (sampled)	—	ρ (sampled)

(i) Chemical oscillators

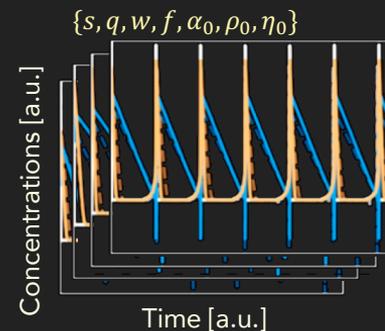
Scheme 1. Subreactions of the Belousov–Zhabotinsky Reaction⁷⁸



Goal: finding parameters which yield a desired dynamic behavior



run experiment →

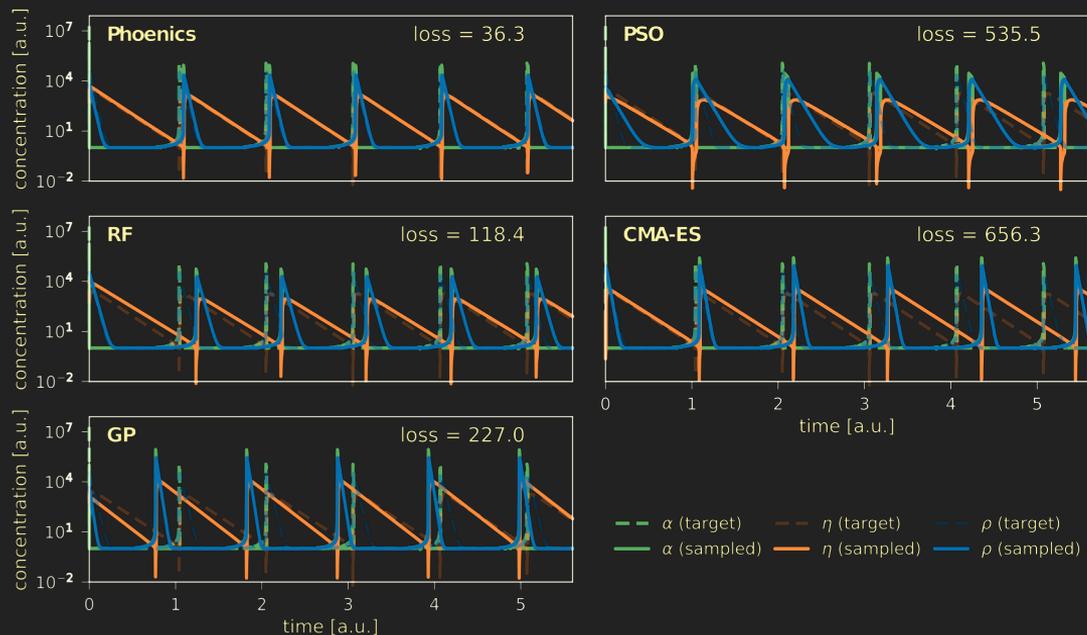
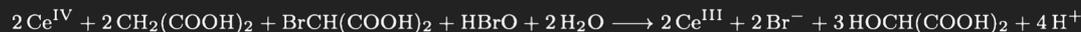
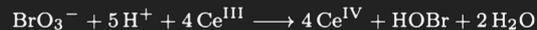
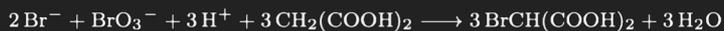


↑ determine merit of suggested parameters

- | | | | | | |
|----|--------------------|----|------------------|----|------------------|
| -- | α (target) | -- | η (target) | -- | ρ (target) |
| — | α (sampled) | — | η (sampled) | — | ρ (sampled) |

(i) Chemical oscillators

Scheme 1. Subreactions of the Belousov–Zhabotinsky Reaction⁷⁸

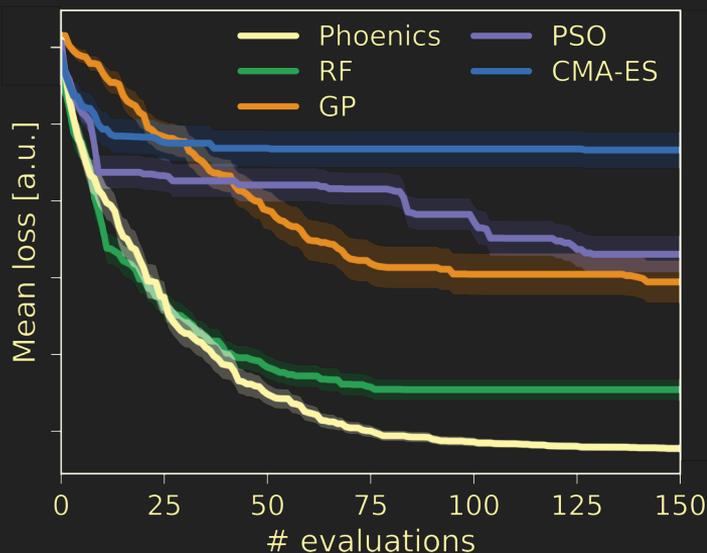
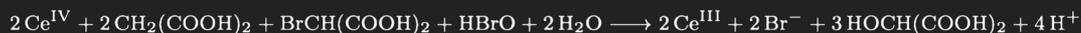
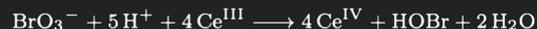


Executed 50 independent runs with a budget of 150 evaluations per run:

- Each set of parameters was integrated for 10^7 steps with adaptive Runge-Kutta scheme
- Compared to *spearmint* (GP), *SMAC* (RF), *particle swarm search* (PSO) and *CMA-ES*
- Inspected traces with best agreement across all runs for each method

(i) Chemical oscillators

Scheme 1. Subreactions of the Belousov–Zhabotinsky Reaction⁷⁸

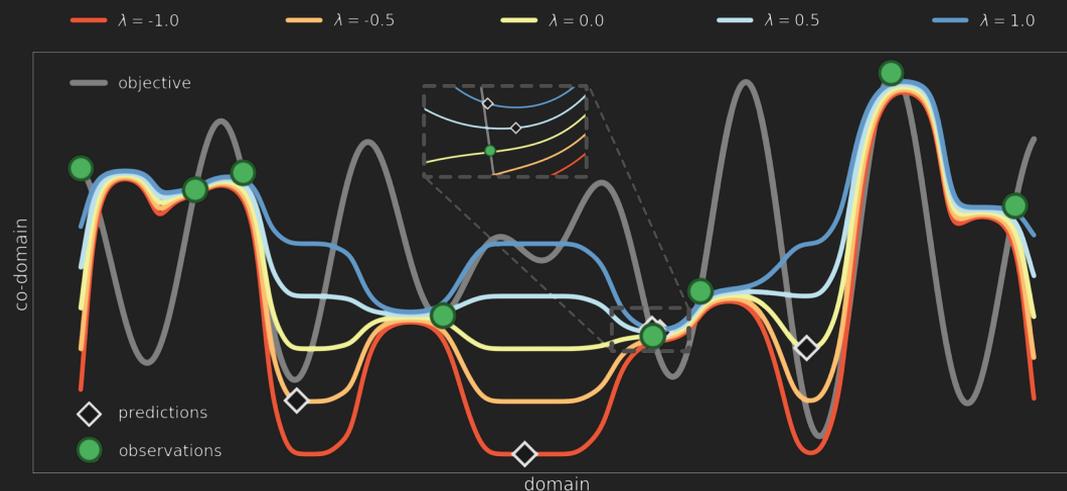
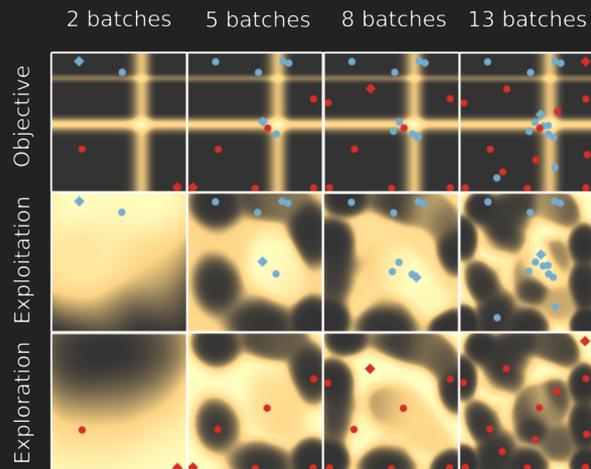


Executed 50 independent runs with a budget of 150 evaluations per run:

- Each set of parameters was integrated for 10^7 steps with adaptive Runge-Kutta scheme
- Compared to *spearmint* (GP), *SMAC* (RF), *particle swarm search* (PSO) and *CMA-ES*
- Average performance of tested optimization algorithms

Summary

Phoenix is a global optimization algorithm inspired by *metadynamics*, which combines ideas from *Bayesian optimization* with concepts from *Bayesian kernel density estimation*.



Acknowledgments

Aspuru-Guzik group

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Brabec group

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José Darío Perea

Thomas Heumüller
Christoph Brabec

Hein group

Lars Yunker
Elena Liles

Sebastian Steiner
Jason Hein

Berlinguette group

Fraser Parlane
Ben MacLeod

Maddie Eghtesad
Curtis Berlinguette

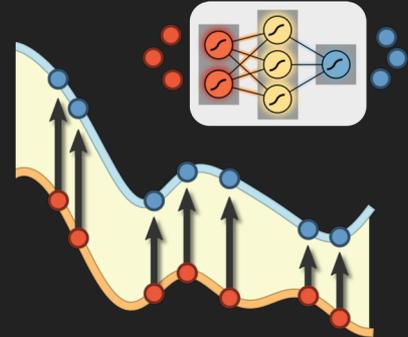


Aspuru-Guzik group (incomplete)

Discussion Points

Providing domain knowledge

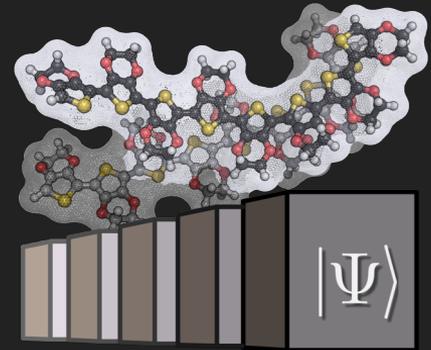
- How can we exploit knowledge acquired from related experiments?
- How can we provide scientific expectations?



Knowledge transfer from related experiments

Interpreting algorithmic choices

- Can we improve on existing methods for analyzing collected experimental data to simplify its interpretation and enable the formulation of (new) scientific concepts?

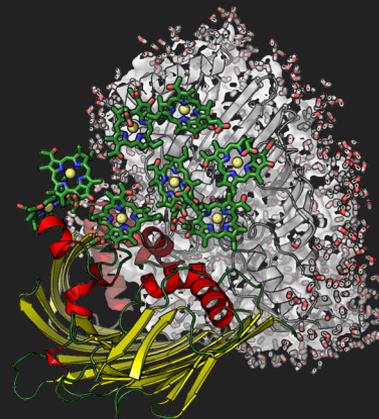
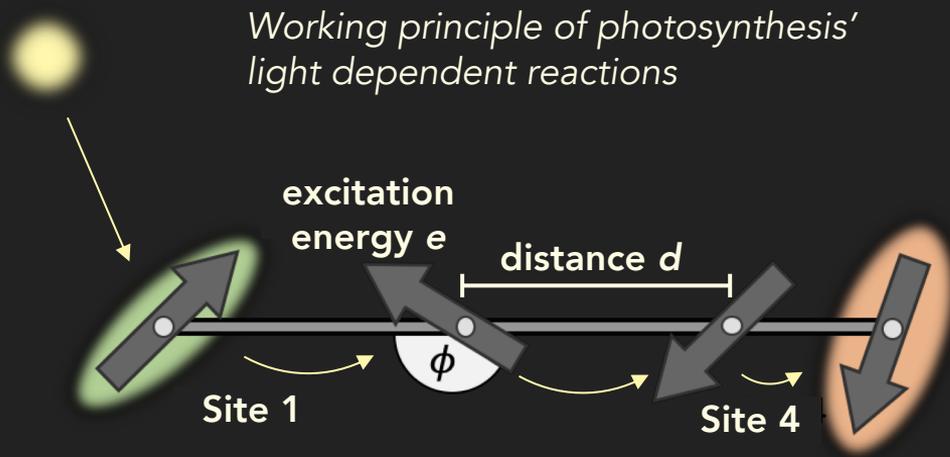


Ab initio calculations of materials properties



(ii) Designing systems for excitation energy transport

- incoming photons locally excite molecular pigments
- excitation is transferred to nearby pigments

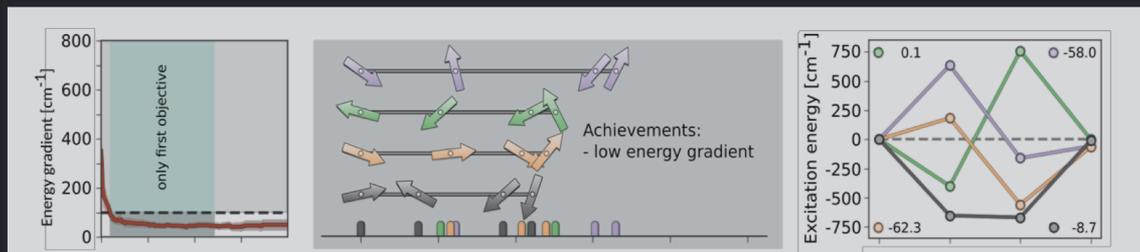


Each system is characterized by:

- **4** transition dipole angles
- **3** excitation energies
- **3** distances between pigments

Total number of parameters: **10**

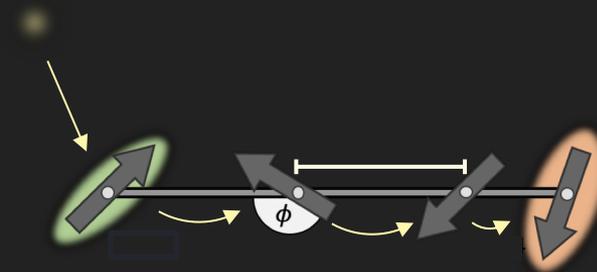
(ii) Designing systems for excitation energy transport



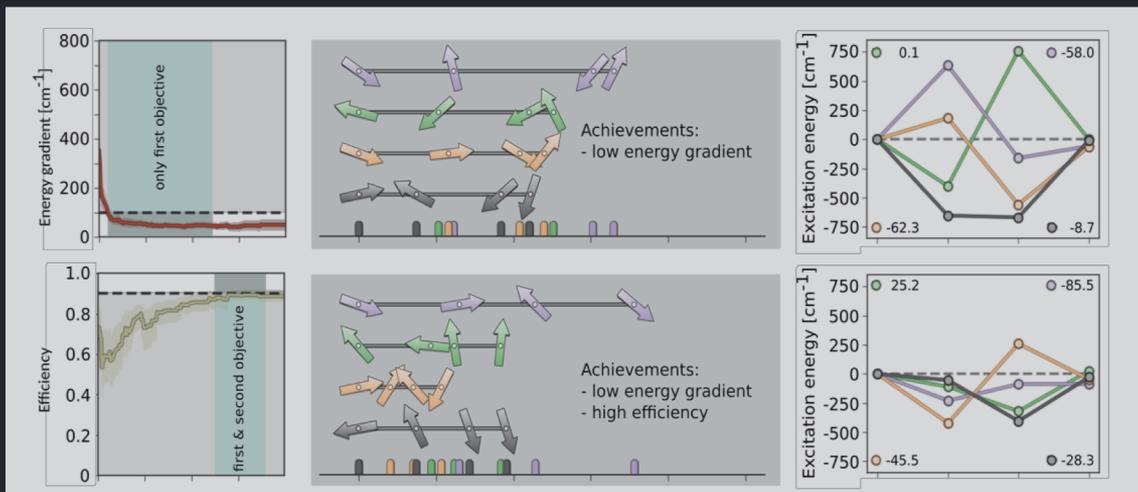
Goal of the optimization:

Small energy gradient

25 independent runs with
400 evaluations per run



(ii) Designing systems for excitation energy transport

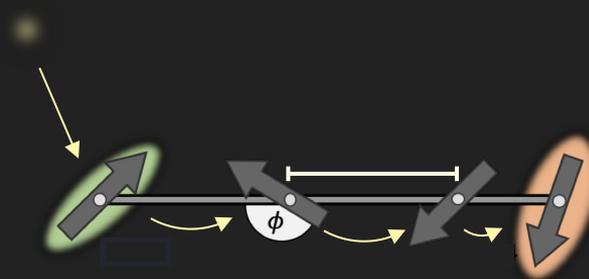


Goal of the optimization:

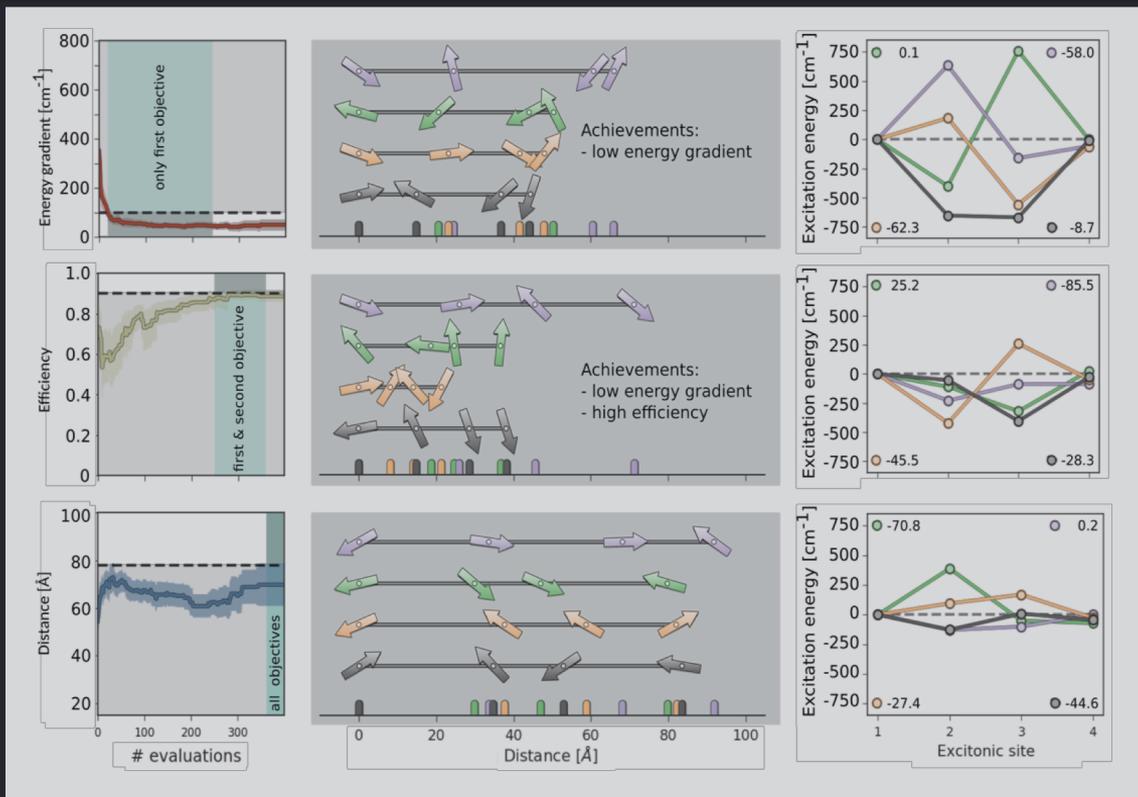
Small energy gradient

Large transfer efficiency

Chimera enables a priori multi-target optimization



(ii) Designing systems for excitation energy transport



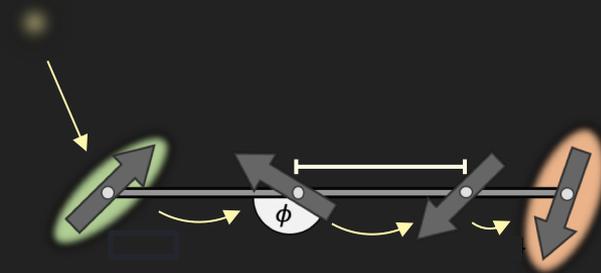
Goal of the optimization:

Small energy gradient

Large transfer efficiency

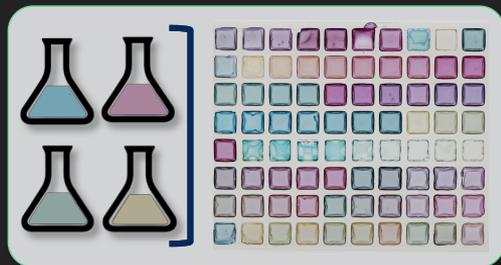
Large total distance

Chimera enables a priori multi-target optimization

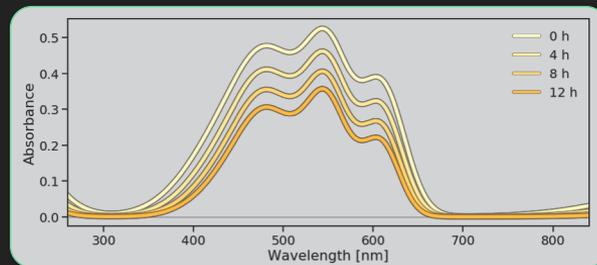


(iii) Designing photostable OPV candidates

Goal: Identify blends for *organic photovoltaics* (OPVs) which do not degrade when exposed to sunlight.



Suggest polymer blend



Measure photo-stability

Direct integration of *Phoenix* with automated platform for OPV fabrication.

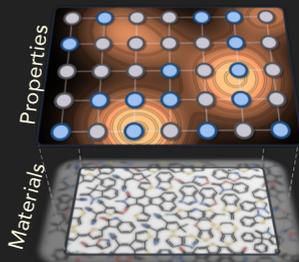
Experiments are conducted in Germany, but remotely controlled from Toronto.



(iii) Designing photostable OPV candidates



High-throughput screening (HTS)



HTS	Phoenics
1022	30
2 blends/ week	9 blends/ week
15 mg/material 100 mL solvent	0.9 mg/material 6 mL solvent
experiments	
throughput	
consumption	

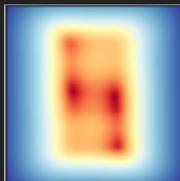


Analytic benchmark functions

Dejong



Camel



Branin



Linear



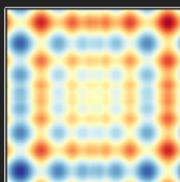
Narrow



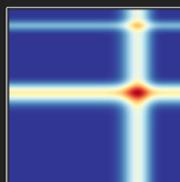
Ellipsoid



Schwefel



Michalewicz



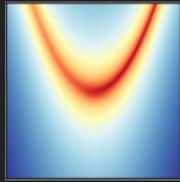
Double



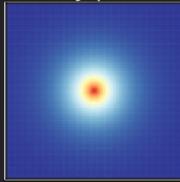
dMichalewicz



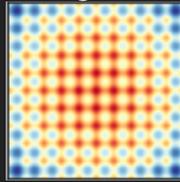
Rosenbrock



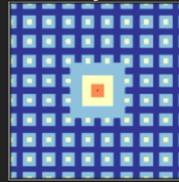
Ackley path



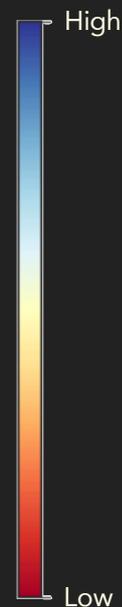
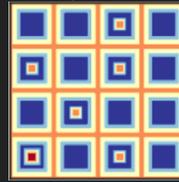
Rastrigin



dAckley



Valleys



Performance on analytic benchmark functions

